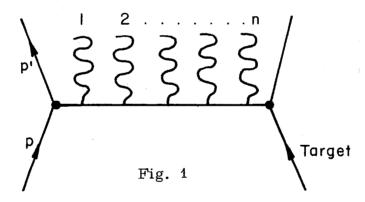
A SIMPLE FORMULA FOR THE DISTRIBUTION OF ENERGETIC SECONDARY BARYONS FROM PROTON-INITIATED COLLISIONS

G. F. Chew and A. Pignotti Lawrence Radiation Laboratory

July 25, 1968

A slight generalization of the multiperipheral model developed by authors in UCRL-18275 leads to a simple formula for the energy-angular distribution of the most energetic secondary baryons from protoninitiated collisions. The multiperipheral diagram is that of Fig. 1, corresponding to the production of n pions together with



the energetic non-strange baryon p, which may be either a nucleon or a low-mass resonance.

In the model of UCRL-18275 let us integrate over all variables except the two referring to the left-most link in Fig. 1. These two remaining variables we here call x and t, rather that x_1 and t_1 . The differential cross section is then (e $^{\circ}$ = E_{lab}/M_p)

$$\frac{\partial^{2} \sigma^{p \to p'}}{\partial x \partial t} \approx \sigma^{p \to p'}_{tot} \left(g^{2}\right)^{n} \quad \left(\frac{X_{o} - x}{o}\right)^{n-1} \quad \bar{a} \quad e^{at} \quad e^{-g^{2}} X_{o}, \quad (1)$$

where we have dropped the M subscript of UCRL-18275, restricting ourselves to the simple model of Sec. E of that paper, where all trajectories are of the "meson" class, none of the Pomeranchuk. We have here inserted a simple exponential t-dependence with a width determined by the parameter a, which may be taken as a constant--or in a better approximation, equal to $a_0 + 2\alpha'x$ where $\alpha' \approx 1 \text{ GeV}^{-2}$ is the slope of the average trajectory. Note that g^2 determines both the energy and multiplicity dependence of the cross section. In particular, $\bar{n} = g^2 X_0$. Note also that if we integrate Formula (1) over dx (from 0 to X_0) and over dt (from 0 to $-\infty$), we find

$$\sigma_{n} \approx \sigma_{\text{tot}}^{p \to p'} = \frac{\left(g^{2}X_{o}\right)^{n}}{n!} = e^{-g^{2}X_{o}}.$$
 (2)

Finally, if we sum Formula (2) over all n, we get $\sigma_{tot}^{p \to p'}$ as the energy-independent total cross section for the proton to produce the baryon p'. Alternately we may first sum Formula (1) over n to obtain

$$\frac{\partial^2 \sigma^{p \to p'}}{\partial x \partial t} \approx \sigma^{p \to p'}_{tot} g^2 e^{-g^2 x} \bar{a} e^{at}. \tag{3}$$

If the x-dependence of a is neglected, we see that the dependence on t and the dependence on x are independent of each other.

The variable t is approximately related to the transverse momentum of the final baryon p':

where $p_{\perp}^{2} \approx -\left(t - t_{\min}\right)$ $-t_{\min} \approx \left(m_{p'}^{2} - m_{p}^{2}\right) \frac{s_{r}}{s}$ (4)

if s_r is the square of the invariant mass of all outgoing particles <u>except</u>
p'. The longitudinal momentum of the final baryon, either in the lab
or c.m. systems, is given by

$$p'_{\parallel} \approx p_{a} \left(1 - \frac{s_{r}}{s}\right)$$
.

What we need, finally, is the relation between s and x. This is given by

$$\frac{s}{s} \approx k e^{-x}, \qquad (5)$$

where k is a constant near unity that depends on dynamical details of the multiperipheral chain. The model fails for x very close to zero, so we cannot determine k by normalization at x = 0. In terms of p'_{\perp} and p'_{\parallel} , the distributions are

$$\frac{\partial \sigma}{\partial \left(p_{\perp}^{\prime}\right)^{2}} \sim e^{-a \left(p_{\perp}^{\prime}\right)^{2}}$$
,

$$\frac{\partial \sigma}{\partial p_{||}^{\prime}} \sim \left(p_{a} - p_{||}^{\prime}\right)^{g^{2} - 1}, \frac{p_{||}^{\prime}}{p_{a}} > 1 - k.$$

The model thus contains four parameters, $\sigma_{\text{tot}}^{p \to p'}$, g^2 , a_o , and k, but g^2 is a universal constant which has been determined to be approximately 1.5 by fitting overall energy multiplicity data. We may estimate a_o by realizing that the average value of x is $X_o/n + 1$, while the average value of $(t - t_{\min})$ is a^{-1} . For n = 3 at 28.5 GeV, and thus $< x > \approx 1$, \bar{p}_{\perp} for outgoing protons is ≈ 0.34 GeV/c. Thus

$$\bar{a} = a_0 + 2\alpha' \approx 9 \text{ GeV}^{-2}, \text{ or } a_0 \approx 7 \text{ GeV}^{-2}.$$
 (6)

The value of k can be obtained from the experimental mean inelasticity factor

$$\left\langle \frac{p_{\parallel}'}{p_{a}} \right\rangle \approx 0.6 , \qquad (7)$$

which from (5) and (6) tells us that

$$k e^{-\langle x \rangle} \approx 0.4. \tag{8}$$

Now the average n is g^2X_0 , so the overall average value of x is roughly independent of X_0 :

$$< x > = {X_0 \over < n > + 1} = {X_0 \over g^2 X_0 + 1} \approx {1 \over g^2} \approx 0.67$$
 (9)

Thus

$$k \approx 0.4 e^{-0.67} \approx 0.8$$
 (10)

The coefficient $\sigma_{tot}^{p\to p'}$ can be determined by measuring at any given energy the total cross section for producing energetic baryons of the type p'.

The spectrum of secondary pions is also well defined in the multiperipheral model but cannot be so easily expressed as in the simple Formula (1). It could easily be calculated on a numerical basis.